Question #0 Alpha Ciphering MA0National Convention 2007

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Question #1 Alpha Ciphering MAONational Convention 2007

The sum of the solutions to the equation:  $x^2 \log 2 + 5x = \log 64 + 5x \log 5$  is an integer **K**. What is the value of **K**? Question #1 Alpha Ciphering MAONational Convention 2007

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Question #3 Alpha Ciphering MA0National Convention 2007

Find the sum of the solutions of  $\tan x \sin x - 1 - \sin x + \tan x = 0$  over  $[0, 2\pi)$ . Question #3 Alpha Ciphering MAONational Convention 2007

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Find the area of the quadrilateral whose vertices are the two foci and the endpoints of the minor axis of the following ellipse:  $3x^2 + 2y^2 - 24x + 12y + 60 = 0$  Question #4 Alpha Ciphering MA0National Convention 2007

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Question #5 Alpha Ciphering MA0National Convention 2007

Find the "sum of the limits":

		1	1
$\lim \frac{3-\sqrt{x+6}}{x+6}$ +	lim	x + 4	4
$x \rightarrow 3$ $3-x$	$x \rightarrow 0$	x	

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Find the "sum of the limits":

$$\lim_{x \to 3} \frac{3 - \sqrt{x + 6}}{3 - x} + \lim_{x \to 0} \frac{\frac{1}{x + 4} - \frac{1}{4}}{x}$$

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Question #6 Alpha Ciphering MA0National Convention 2007

$$Matrix A = \begin{pmatrix} 1 & 3 & -2 \\ 2 & 2 & 1 \\ -1 & 1 & 4 \end{pmatrix}.$$

What is the sum of the entries in the third row of  $A^{-1}$ ?

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Question #7 Alpha Ciphering MA0National Convention 2007

5,9,19,35,... is a quadratic sequence that can be expressed in the form  $a_n = An^2 + Bn + C$  for n = 1, 2, ...: What is the value of A - B + C? Question #7 Alpha Ciphering MA0National Convention 2007

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Question #10 Alpha Ciphering MA0National Convention 2007

If  $\cos x + \cos y = \frac{1}{3}$  and  $\sin x - \sin y = \frac{1}{6}$ , find the value of  $\cos(x+y)$ . Question #10 Alpha Ciphering MA0National Convention 2007

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