

**#0 Mu Ciphering**

**MAΘ National Convention 2019**

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Find the equation of the tangent line to the graph  
 $y = \sin x + x$  at the point  $(0, 0)$ .

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A line with negative slope passes through  $(2,0)$  and is tangent to  $\frac{x^2}{2} + \frac{y^2}{1} = 1$ . The line can be written in the form  $y = mx + b$ . Compute  $\frac{b}{m}$ .

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Evaluate the improper integral:

$$\int_{-7}^2 \frac{dx}{(x-1)^{\frac{2}{3}}}$$

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Find the maximum value, on the interval  $\left[0, \frac{\pi}{6}\right]$ , of  
 $y = 24 \sin(3x) + 8 \cos(6x)$ .

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Right triangle  $ZLU$  is inscribed in a circle, with radius 24 and hypotenuse  $\overline{ZL}$ .  $m\angle Z$  is increasing at a rate of  $10^\circ$  per minute as  $U$  moves along the circumference of the circle (while  $Z$  and  $L$  remain fixed). The area of the triangle is changing at  $k\pi$  square units per minute when  $m\angle Z = 30^\circ$ . What is  $k$ ?

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The area bounded by  $y = \arctan x$ ,  $x = 0$ , and  $y = \frac{\pi}{4}$  is  $L$ . Compute  $e^{8L}$ .

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A particle moves along the  $x$ -axis so that  $v(t) = t^2 - 3t$  for  $0 \leq t \leq 4$ . If its position at time 0 is 4, what is the greatest distance between the particle and the origin?

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If a banquet hall sells tickets at a price of  $\$L$  each, then  $200 - 4L$  tickets will be sold. Each event costs the banquet hall  $\$200$ , plus an additional  $\$10$  per person. How much should they charge, in dollars per ticket, to maximize their profit?

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What is the total area between the curves  
 $y = -6x$  and  $y = 6x^2 - 18x$  for  $1 \leq x \leq 3$ ?

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The region bounded by the  $x$ -axis,  $y = x - 2$ , and  $y = \sqrt{x}$  is revolved about the  $x$ -axis. The volume is  $\frac{L\pi}{U}$ , where  $L$  and  $U$  are relatively prime positive integers. What is  $L + U$ ?

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If  $x = t^2$  and  $y = \ln(t^2 + 1)$ , then at  $t = 1$ ,  $\frac{d^2y}{dx^2} = ?$

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The region bounded by  $y = -x^2 + x$  and the  $x$ -axis is L. Region L is the base of a solid, and cross sections of this solid perpendicular to the  $x$ -axis are isosceles right triangles with hypotenuses on L. What is the volume of this solid?

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Let  $f$  and  $h$  be functions satisfying:

$$(h(x))^3 = f^{-1}(6057x - 6057)$$

Compute:

$$(h(x))^2 h'(x) f'((h(x))^3)$$

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