

Answer “E” will be “NOTA” meaning none of the above answers is correct.

1. Find the 4<sup>th</sup> term of  $(3x + 2)^7$ , where terms are written in descending order by power of  $x$ .

- a.  $840x^4$                       b.  $2923x^4$                       c.  $22680x^4$                       d.  $210x^3$                       e. NOTA

2. Find “ $r$ ” such that when  $x^3 + (r - 1)x + 3$  is divided by  $(x + 1)$  the remainder will be 5.

- a. -2                      b. -1                      c. 3                      d. 4                      e. NOTA

3.  $\frac{|2 - 2i|}{|3 + 4i|} = ?$

- a.  $\frac{8\sqrt{3}}{25}$                       b.  $\frac{8\sqrt{3}}{25}i$                       c.  $\frac{2 + 14i}{25}$                       d.  $\frac{2\sqrt{2}}{5}$                       e. NOTA

4. Six distinct integers are selected at random from  $\{2015, 2016, 2017, \dots, 2024\}$ . What is the probability that, among those selected, the second smallest is 2017?

- a.  $\frac{1}{60}$                       b.  $\frac{1}{6}$                       c.  $\frac{1}{3}$                       d.  $\frac{1}{2}$                       e. NOTA

5. Benji the Bug starts at a point  $(x, y)$  on the graph of  $4x^2 + 9y^2 = 36$ . He walks in a straight line to the point  $(\sqrt{5}, 0)$ , then in a straight line to the point  $(-\sqrt{5}, 0)$ , then in a straight line to his original starting point. How far has Benji walked?

- a.  $6 + 2\sqrt{5}$                       b.  $8 + 2\sqrt{5}$                       c.  $10 + 2\sqrt{5}$                       d.  $12 + 2\sqrt{5}$                       e. NOTA

6. The following sequence is a quadratic sequence where any  $n$ th term can be represented by  $a_n = An^2 + Bn + C$                       1, 6, 17, 34, 57, ...                      What is the value of  $A - B + C$ ?

- a. -2                      b. -1                      c. 3                      d. 9                      e. NOTA

7.  $\lim_{n \rightarrow \infty} \frac{3}{n^2} (2 + 4 + 6 + \dots + 2n) = ?$

- a. 2                      b. 3                      c. 4                      d. 6                      e. NOTA

8.  $\sum_{k=3}^{\infty} \frac{8}{(k+2)(k-2)} = ?$ .

- a.  $\frac{23}{6}$                       b.  $\frac{-23}{6}$                       c.  $\frac{25}{6}$                       d.  $\frac{-25}{6}$                       e. NOTA

9. If  $m$  and  $n$  are integers such that  $x^2 - x - 1$  is a factor of  $mx^3 + nx^2 + 1$ , then  $n = ?$

- a. -2                      b. -1                      c. 0                      d. 2                      e. NOTA

10. Simplify:  $\frac{(x^2 - 4y^2 + 4y - 1)(x + 2y)}{(x^2 - x - 4y^2 + 2y)(x^2 + 2y + x - 4y^2)}$

- a.  $x + 2y$                       b.  $\frac{x + 2y}{2}$                       c.  $\frac{1}{(x - 2y)(x + 2y)}$                       d.  $\frac{1}{x - 2y}$                       e. NOTA

11. A 4 liter solution is  $X\%$  acid. If  $\frac{4}{3}$  liters of pure acid are added to this solution, the new solution becomes  $(X + 20)\%$  acid. What percent of the new solution is pure acid?

- a. 20                      b. 40                      c. 85                      d. Not possible                      e. NOTA

12. Given matrix  $A = \begin{pmatrix} -3 & -4 \\ 7 & 9 \end{pmatrix}$  Find the value of

$\left[ \det(A^{-1}) + \text{the first row, second column entry of } A^{-1} \right]$ .

- a. -57                      b. -50                      c. -6                      d. 5                      e. NOTA

13. Find the sum of the solutions for the following equation:  $9^{x-1} - 3^{x-1} - 2 = 0$

- a.  $\emptyset$                       b.  $\log_3 6$                       c.  $\log_6 3$                       d.  $\log_9 6$                       e. NOTA

14. The number of solutions to  $\{L, U\} \subseteq X \subseteq \{M, R, Z, L, U\}$ , where  $X$  is a set, is?

- a. 2                      b. 4                      c. 6                      d. 8                      e. NOTA

15. Find the length of the latus rectum of:  $y^2 - 16x - 4y - 60 = 0$

- a.  $\frac{1}{4}$                       b.  $\frac{1}{16}$                       c. 8                      d. 32                      e. NOTA

16. What is the sum of an infinite geometric series in which the 1<sup>st</sup> term is 1 and the common ratio is  $-\sqrt{2}$  ?

- a. Undefined                      b.  $\sqrt{2} - 1$                       c.  $\sqrt{2} + 1$                       d.  $\frac{\sqrt{2}}{2}$                       e. NOTA

17. Describe the steps of:  $f(x) = \frac{1}{2}[3x]$ , where  $[ ]$  represents the greatest integer function.

- a.  $\frac{1}{2}$  unit apart vertically, 3 units long                      b. 3 units apart vertically, 2 units long  
 c.  $\frac{1}{2}$  unit apart vertically,  $\frac{1}{3}$  units long                      d. 2 units apart vertically, 3 units long                      e. NOTA

18. Given polynomial  $P(x) = x^4 + ax^3 + bx^2 + c$ . If  $P(2) = 1$ ,  $P(3) = 11$ , and  $P$  is an even function, then what is the value of  $a + b + c$  ?

- a. 11                      b. 18                      c. 22                      d. 25                      e. NOTA

19. If  $\frac{4 + 4^2 + 4^3 + \dots + 4^{10}}{4^{-1} + 4^{-2} + 4^{-3} + \dots + 4^{-10}} = 4^n$  then  $n = ?$

- a. 0                      b. 1                      c. 10                      d. 11                      e. NOTA

20. What is the domain of  $y = \log\left(\frac{1}{\sqrt{x^2 - 4}}\right)$  ?

- a.  $(-\infty, -2] \cup [2, \infty)$                       b.  $(-\infty, -2) \cup (2, \infty)$                       c.  $[2, \infty)$                       d.  $(2, \infty)$                       e. NOTA

21. If  $\sin x = \frac{2}{5}$  and  $\sin 3x = \frac{L}{U}$  where  $L$  and  $U$  are relatively prime positive integers, what is  $|L - U| = ?$

- a. 3                      b. 5                      c. 7                      d. 9                      e. NOTA

22. Determine which of the following angles is supplementary to 2.1 (round to two decimals).

- a. 167.90°                      b. 168.10°                      c. 1.04                      d. 4.18                      e. NOTA

23.  $\sin\left(\sin^{-1}\left(\frac{3}{5}\right) - \cos^{-1}\left(\frac{12}{13}\right)\right) = ?$

- a.  $-\frac{33}{65}$                       b.  $\frac{16}{65}$                       c.  $\frac{56}{65}$                       d.  $\frac{36}{65}$                       e. NOTA

24. Suppose for the state of Florida in any 5-year period the probability of a major hurricane is .25, the probability of a major freeze is .44, and the probability of both a major hurricane and a major freeze is .22. What is the probability of a major freeze given that there is a major hurricane (round to two decimals)?

- a. 0.47                      b. 0.50                      c. 0.69                      d. 0.88                      e. NOTA

25. A piece of beef jerky is located at (12,10). Buffy is at (4,-2) and is running up the line  $y = -5x + 18$ . At the point (k,n) Buffy starts getting farther from the beef jerky rather than closer to it. What is k + n?

- a. 6                      b. 10                      c. 14                      d. 18                      e. NOTA

26. For what value of k is  $i + 2i^2 + 3i^3 + \dots + ki^k = 48 + 49i$ ?

- a. 48                      b. 49                      c. 97                      d. 98                      e. NOTA

27. If  $\begin{cases} |L| + L + U = 10 \\ L + |U| - U = 12 \end{cases}$  what does  $L+U=?$

- a. -2                      b.  $\frac{18}{5}$                       c.  $\frac{22}{3}$                       d. 22                      e. NOTA

28. If  $\sin x + \sin y = \frac{\sqrt{15}}{3}$  and  $\cos x + \cos y = 1$ , what is  $\cos(x-y)$ ?

- a.  $\frac{1}{3}$                       b.  $\frac{1}{2}$                       c.  $\frac{2}{3}$                       d. 1                      e. NOTA

29. The perimeter of an equilateral triangle is numerically equivalent to the area enclosed by its circumscribed circle. What is the diameter of the circle?

a.  $\frac{6\sqrt{2}}{\pi}$

b.  $\frac{6\sqrt{3}}{\pi}$

c.  $\frac{12}{\pi}$

d.  $2\pi\sqrt{3}$

e. NOTA

30. Find the distance between the points with polar coordinates:  $\left(3, \frac{5\pi}{6}\right)$  and  $\left(5, \frac{5\pi}{3}\right)$ .

a.  $\sqrt{34+15\sqrt{3}}$

b.  $\sqrt{34-15\sqrt{3}}$

c.  $\sqrt{16+15\sqrt{3}}$

d.  $\sqrt{16-15\sqrt{3}}$

e. NOTA