Theta Conic Sections

Choice E, "NOTA", means "none of these answers".

- 1. What is the radius of the figure defined by the equation $x^2 + y^2 + 8x 6y 15 = 0$?
 - A) 10 B) $2\sqrt{10}$ C) 20 D) 40 E) NOTA

2. What is the length of the major axis of the figure defined by the following: $36x^2 + 9y^2 = 324$?

A) 3 B) 6 C) 9 D) 12 E) NOTA

3. What is the vertex of the figure defined by the equation $y^2 - 6y + 32x - 23 = 0$?

A) (1, -3) B) (-3,1) C) (1, 0) D) (1, 3) E) NOTA

4. What is the center of the figure defined by the equation $x^2 + y^2 + 14x - 2y - 94 = 0$?

- A) (-7, 1) B) (7, 1) C) (-7, 2) D) (7, -1) E) NOTA
- 5. What type of conic section is defined by the equation $9x^2 36x + 9 = y^2 6y 18$?
 - A) Circle B) Ellipse C) Hyperbola D) Parabola E) NOTA
- 6. Which of the following is the equation of the parabola which has vertex at (2, 1) and focus at (2, 4)?

A)
$$y^2 + 6y + 9 + 16x = 16$$
 B) $y = \frac{1}{4}x^2 - x + 2$ C) $y = \frac{1}{12}(x^2 - 4x - 8)$ D) $y = \frac{1}{12}(x^2 + 4x + 16)$ E) NOTA

- 7. What is the equation of the directrix of the parabola which has vertex at (1, -3) and focus at (-3, -3)?
 - A) y = -3 B) x = 2 C) x = 5 D) y = 5 E) NOTA
- 8. Find the length of the radius of the circle that is tangent to the line 5x 3y = 7, and has center at (-3, 4).
 - A) $2\sqrt{7}$ B) $\sqrt{34}$ C) 6 D) $3\sqrt{5}$ E) NOTA
- 9. Which of the points listed below is one of the foci of the ellipse $3x^2 + 4y^2 6x + 16y + 7 = 0$?
 - A) (0, -2) B) $(1+\sqrt{7}, -2)$ C) (-4, -2) D) (1, -1) E) NOTA

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10. What is the length of the transverse axis of the hyperbola with equation $9x^2 - 90x - 16y^2 + 64y + 17 = 0$?								
A)	6	B) 8	C) 9	D) 16	E) NOTA			
11. What geometric figure is defined by the following equation: $6x = y^2 - 2y + x^2 - 5$?								
A)	circle	B) ellipse	C) hyperbola	D) parabola	E) NOTA			
12. A diameter of a circle has endpoints at (-2, 3) and (6, 5). What is the area enclosed by this circle?								
A)	68π	B) 20π	C) 17π	D) 10π	E) NOTA			
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13. Which of the following points is the focus of the parabola $y^2 - 4y - 4x = 0$?								
A)	(-1, 1)	B) (-1, 3)	C) (2, -1)	D) (0, 2)	E) NOTA			
14. Which of the equations below represents one of the asymptotes of the graph of $4x^2 - 24x - 9y^2 - 36y = 36$?								
A)	3x - 2y = 5	B) $2x - 3y = 0$	C) $2x - 3y = 12$	D) $2x + 3y = 12$	E) NOTA			
15. An ellipse has foci at (3, 4) and (3, -2); the length of the minor axis is 8. What is the area enclosed by this ellipse?								
A)	12π	B) 15π	C) 20π	D) 25π	E) NOTA			
16. Find the area enclosed by the circle that passes through the points $(-2, 3)$, $(6, -5)$, and $(0, 7)$.								
A)	50π	B) 25π	C) 48π	D) 24π	E) NOTA			

17. A point P moves across the coordinate plane on a path such that the sum of the distances from the P to (5, -1) and (5, 3) is 8. Which equation below describes the path of point P ?

A) $3(x-5)^2 + 4(y-1)^2 = 12$ B) $(x-5)^2 + 2(y-1)^2 = 12$ E) NOTA C) $4(x-5)^2 + 3(y-1)^2 = 48$ D) $3(x-5)^2 + 4(y-1)^2 = 48$

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- 18. Which of the following points is a vertex of the graph of $25x^2 4y^2 + 100x + 24y = 36$
 - A) (-4,3) B) (2,3) C) (-2,5) D) (-4,1) E) NOTA
- 19. What is the eccentricity of the conic section whose equation is $\frac{(x-3)^2}{4} + \frac{(y+4)^2}{25} = 1$?
 - A) $\frac{21}{25}$ B) $\frac{\sqrt{21}}{5}$ C) $\frac{4}{25}$ D) $\frac{4}{21}$ E) NOTA

20. Which of the following is the graph of $3x^2 - 12x + 4y^2 - 8y + 16 = 0$?

- A) a point B) a hyperbola C) 2 intersecting lines D) an ellipse E) NOTA
- 21. Find the *x*-intercept of the line that is tangent to the graph of $x^2 = 2y$ at the point (-3, 4.5).
 - A) 4.5 B) -1.5 C) -4.5 D) 0.5 E) NOTA
- 22. The center of an ellipse is (-1, 8), and one of its vertices is (-1, 17). The length of the minor axis is 6. Which of the following represents the equation of this ellipse?
 - A) $x^{2} + 2x + 9y^{2} 144y + 495 = 0$ B) $4x^{2} + 8x + y^{2} - 16y + 28 = 0$ C) $9x^{2} + 18x + y^{2} - 16y - 16 = 0$ E) NOTA D) $9x^{2} + 18x + y^{2} - 16y - 8 = 0$
- 23. What is the length of the conjugate axis of $9x^2 + 72x 25y^2 + 100y + 269 = 0$?
 - A) 10 B) 9 C) 1 D) does not exist E) NOTA
- 24. A parabola has *x*-intercepts at (2, 0) and (4, 0) and a *y*-intercept of -8. Which of the following is the focus of this parabola?
 - A) $\left(3, \frac{7}{4}\right)$ B) $\left(3, \frac{5}{4}\right)$ C) $\left(3, 1\right)$ D) $\left(3, \frac{3}{4}\right)$ E) NOTA

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- 25. Find the *x*-intercept of the line which is tangent to the circle $x^2 + y^2 = 10$ at the point (-1,3).
 - A) $\frac{10}{3}$ B) 3 C) -10 D) 0 E) NOTA

26. A parabola with a horizontal axis of symmetry passes through the point (3, 3) and has its vertex at (4, 1). What is the arithmetic mean of the *y*-intercepts of this parabola?

A) cannot tell B) 4 C) 0 D) 1 E) NOTA

27. What is the sum of the *y*-intercepts of the asymptotes of the graph of $\frac{(y-3)^2}{25} - \frac{(x-2)^2}{16} = 1$?

- A) -6 B) -5 C) 0 D) 5 E) NOTA
- 28. Which of the following is the directrix of the parabola $y^2 12x 2y + 25 = 0$?
 - A) y = -1 B) x = -1 C) x = 5 D) y = 2 E) NOTA

29. A parabola has focus at (4, -3) and directrix of y = 6. Find the length of the latus rectum of this parabola.

- A) $\frac{2}{9}$ B) $\frac{9}{2}$ C) 9 D) 18 E) NOTA
- 30. Which describes the locus of points that are equidistant from a fixed point and a line?

A) ellipse	B) parabola	C) hyperbola	D) a plane	E) NOTA
/r~-	_/ F	- / <i>J</i> F	_ / F	