Choice E, "NOTA", means "none of these answers".

- 1. Find the product of the coordinates of the point at which the lines 2x + 3y = 8 and 5x + 2y = -2 intersect.
  - A) -8 B) -4 C) 8 D) 40 E) NOTA
- 2. What is the equation of the line that contains the point (20, -17) and has undefined slope?
  - A) y = -17 B) 20x 17y = 0 C) x = 20 D) x = 0 E) NOTA
- 3. Given the equation  $\frac{1}{x^2 2x 3} = \frac{A}{x 3} + \frac{B}{x + 1}$ , where *A* and *B* are real, find the value of the product *AB*.
  - A) 1 B) -2/3 C) 3/2 D) -1/16 E) NOTA

4. Given  $x^2 + y^2 \le 3$  with x and y both integers, how many ordered pairs (x, y) satisfy this inequality?

A) 4 B) 6 C) 7 D) 8 E) NOTA

5. Given  $y = 2^{x+2} - (2^{x+1} + 2^x)$ , which of the following is an equivalent expression for y?

A) 
$$2^{-x+1}$$
 B)  $\frac{2^{x+2}}{2^{2x+1}}$  C)  $2^x$  D)  $\frac{1}{2^{x+1}}$  E) NOTA

6. Given that  $\sqrt{9+4\sqrt{5}} = \sqrt{x} + \sqrt{y}$ , with *x* and *y* both positive rational numbers and *x* < *y*, find the value of the expression 3x - y.

- A) 7 B) 17 C) 20 D) no solution E) NOTA
- 7. Find the distance between the foci of  $4x^2 + 9y^2 + 24x 72y + 144 = 0$ .
  - A) 1 B)  $2\sqrt{2}$  C)  $2\sqrt{5}$  D) 4 E) NOTA
- 8. What is the *x*-intercept of the perpendicular bisector of the segment with endpoints (5, -2) and (-7, -6)?
  - A) -7 B)  $-\frac{7}{3}$  C)  $-\frac{11}{3}$  D) 11 E) NOTA

9. Given that x + y = 11 and  $x^2 + y^2 = 325$ , find the value of the expression  $x^3 + y^3$ .

A) 2,453 B) 3,575 C) 4,697 D) 5,113 E) NOTA

Theta

- 10. What is the greatest integer contained in the solution set of  $-3(x-2) x(x-3) < -x^2 2x 8$ ?
  - A) 0 B) -6 C) -7 D) -8 E) NOTA
- 11. Consider the polynomial equation of least degree with coefficients that are relatively prime integers. The known roots of this equation are 2 + i,  $-\frac{3}{2}$ , and *i*. Find the coefficient of the quadratic term of this equation in expanded form.
  - A) 16 B) 15 C) 10 D) -5 E) NOTA

12. Solve for  $x \frac{x^2 - 2x - 3}{x - 1} \ge 0$  and express the solution in interval notation.

- A)  $[3,\infty)$  B)  $(-\infty,-1] \cup (1,3)$  C)  $(-1,1) \cup (3,\infty)$  D)  $[-1,1] \cup [3,\infty)$  E) NOTA
- 13. What is the sum of the integral solutions of  $|4x-5| \le x+8$ ?
  - A) 10 B) 6 C) 53/20 D) infinite E) NOTA
- 14. Which matrix equation is not equivalent to the system  $\frac{5x+2y=-3}{4x-3y=7}$ ?
  - $A)\begin{bmatrix}5x\\4x\end{bmatrix} + \begin{bmatrix}2y\\-3y\end{bmatrix} = \begin{bmatrix}-3\\7\end{bmatrix} \quad B)\begin{bmatrix}-3&4\\2&5\end{bmatrix} \cdot \begin{bmatrix}y\\x\end{bmatrix} = \begin{bmatrix}7\\-3\end{bmatrix} \quad C)\begin{bmatrix}5&2\\4&-3\end{bmatrix} \cdot \begin{bmatrix}x\\y\end{bmatrix} = \begin{bmatrix}-3\\7\end{bmatrix} \quad D)\begin{bmatrix}5x+2y\\4x-3y\end{bmatrix} = \begin{bmatrix}-3\\7\end{bmatrix} \quad E) \text{ NOTA}$
- 15. Find the equation of the line tangent to the circle  $x^2 + y^2 + 2x 4y = 15$  at the point (3, 4).
  - A) 2x + y = 5 B) 2x + y = 10 C) x 2y = 5 D) x 2y = -5 E) NOTA

16. Find the area of the region bounded by the intersection of the graphs of  $x \le 3$  and  $\frac{(x-3)^2}{16} + \frac{(y+2)^2}{4} \le 1$ .

- A)  $32\pi$  B)  $8\pi$  C)  $4\pi$  D)  $\pi$  E) NOTA
- 17. What is the minimum value of the function  $f(x) = 3x^2 + 24x + 35$ ?
  - A) -13 B) -8 C) -4 D) 179 E) NOTA

18. If  $f(x) = 2017^x$ , then f(x+1) - f(x) is equivalent to which of the following?

- 19. What is the product of the solutions of the equation  $x^{\log x} = 100x$ ?
  - A) -10 B) -2 C) 10 D) 100 E) NOTA
- 20. Which if the following is the inverse of the function f(x) = 3x + 5?

A) 
$$f^{-1}(x) = \frac{x+5}{3}$$
 B)  $f^{-1}(x) = \frac{x-5}{3}$  C)  $f^{-1}(x) = \frac{x-3}{5}$  D)  $f^{-1}(x) = \frac{5-x}{3}$  E) NOTA

21. Find the value of the sum of the two intertwined geometric series given by  $\frac{5}{2} - \frac{1}{3} + 1 + \frac{2}{9} + \frac{2}{5} - \frac{4}{27} + \dots$ A)  $\frac{983}{270}$  B)  $\frac{19}{6}$  C)  $\frac{13}{10}$  D)  $\frac{119}{30}$  E) NOTA

- 22. The Davis family has 5 children. It is known that at least 3 of the children are boys. What is the probability that there are 3 boys and 2 girls?
  - A)  $\frac{1}{3}$  B)  $\frac{1}{4}$  C)  $\frac{5}{8}$  D)  $\frac{5}{16}$  E) NOTA

23. Suppose the value of an antique chair varies inversely with the number of such chairs that still exist. If 1,200 exist, each chair has a value of \$420. How much would each chair be worth if only 75 still exist?

- A) \$6,720 B) \$13,440 C) \$19,200 D) \$20,160 E) NOTA
- 24. The zeros of the function  $f(x) = x^3 + 2nx^2 nx + 10$  are integers and form an arithmetic sequence. Find the value of f(-3).
  - A) -100 B) -80 C) -8 D) 8 E) NOTA
- 25. Let k = the constant term of the expansion of  $\left(2x^2 \frac{1}{x}\right)^9$ . What is the value of k?
  - A) 8 B) 168 C) 448 D) 672 E) NOTA

26. If 
$$A = \begin{bmatrix} 2 & -1 \\ -4 & 3 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -3 & 0 \\ 2 & -2 \end{bmatrix}$ , find the sum of the elements of the product  $(A^{-1})(B^2)$ .

A) 51 B) 45 C) 22.5 D) -7.5 E) NOTA

27. Which of the following is the sum of the *y*-intercepts of the asymptotes of  $4x^2 - 24x - y^2 - 4y + 41 = 0$ ?

- A) 12 B) 4 C) -4 D) -12 E) NOTA
- 28. Consider the function  $R(x) = \frac{2x^2 + x 6}{x^2 3x 10}$ . What is the length of the segment whose endpoints are the point of removable discontinuity of R(x) and the intersection point of the horizontal and vertical asymptotes of R(x)?
  - A)  $5\sqrt{2}$  B)  $\sqrt{10}$  C)  $4\sqrt{2}$  D) 4 E) NOTA
- 29. Solve for x over the set of Reals:  $(e^{\ln(x-1)})(\ln e^{(x+5)}) = 3(\ln e) + e^{2(\ln 2)}$ A) 2 B) 3 C) 5 D) 6 E) NOTA
- 30. Find the sum of the solutions of  $\sqrt{2x+6} \sqrt{x+4} = 1$  over the set of Real numbers.
  - A) 5 B) 2 C) -2 D) Ø E) NOTA