#### #0 Theta Ciphering MA⊕ National Convention 2016

Find the fifth term of the expansion of  $(2x-1)^7$ , where the terms are written in descending order of the exponent of x.

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#### #1 Theta Ciphering MA⊖ National Convention 2016

Solve for *x*:

$$\left(\frac{4}{9}\right)^{2x+7} = \left(\frac{27}{8}\right)^{x+3}$$

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#### #2 Theta Ciphering MA⊚ National Convention 2016

Given  $x^2 - y^2 = 7$  and x + y = -1, find the value of 5x + 6y - 3xy.

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### #3 Theta Ciphering

#### MA® National Convention 2016

Solve for real *x*, where all expressions are real:

$$\sqrt{3x} + \sqrt{2x - 1} = \frac{5}{\sqrt{2x - 1}}$$

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#### #4 Theta Ciphering MA⊕ National Convention 2016

Evaluate:  $3(\log 4)(\log 25)^2 + (\log 25)^3 + (\log 4)^3 + 3(\log 4)^2(\log 25)$ 

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### #5 Theta Ciphering MA⊕ National Convention 2016

Find the distance between the vertex of

$$y = \frac{1}{2}x^2 - 6x + 15$$
 and the center of

$$x^2 - 4x + y^2 - 6y = 5$$
.

### #5 Theta Ciphering MA⊕ National Convention 2016

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#### #6 Theta Ciphering MA⊕ National Convention 2016

Two numbers *x* and *y* have a geometric mean of 12 and an arithmetic mean of 12.5. Find the sum of the squares of *x* and *y*.

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#7	Theta Ciphering	
ΜA	<b>National Convention</b>	2016

Write  $2016_{10}$  as a base 4 numeral.

# #7 Theta Ciphering MA® National Convention 2016

Write 2016<sub>10</sub> as a base 4 numeral.

**#7 Theta Ciphering** MA⊚ National Convention 2016

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#### #8 Theta Ciphering MA⊕ National Convention 2016

Todd and Calvin start cycling from the same point but in perpendicular directions. Todd and Calvin are traveling at 30 miles/hour and 24 miles/hour, respectively, and they travel for 48 minutes and 25 minutes, respectively. They then both begin at the same time traveling toward each other, both at 12 miles/hour. How many minutes will it take them to meet?

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#### #9 Theta Ciphering MA⊕ National Convention 2016

Two vertical poles are 32 feet apart at their bases. The height of the two poles are 40 feet and 24 feet. From the top of each pole, a wire is stretched to the base of the opposite pole. At what height above the ground, in feet, do the two wires cross one another?

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#### #10 Theta Ciphering MA⊕ National Convention 2016

Find the *x*-intercept of the line that is perpendicular to 5x-2y=6 and passes through the midpoint of the line segment whose endpoints are (-5,-3) and (-1,7).

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### #11 Theta Ciphering MA® National Convention 2016

A regular hexagon is circumscribed about a circle whose radius has length 9 units. Find the area of the region inside the hexagon and outside the circle.

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#### #12 Theta Ciphering MA⊕ National Convention 2016

A triangle has a circumscribed circle whose radius is 8 more than twice the length of the radius of the triangle's inscribed circle. If the distance between the centers of these two circles is 12, find the length of the radius of the circumscribed circle.

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### #13 Theta Ciphering

#### MA® National Convention 2016

Solve for 
$$x$$
: 
$$\begin{vmatrix} 1 & x & 2 \\ 2 & 3 & 0 \\ 0 & -1 & 2 \end{vmatrix} = \begin{vmatrix} 0 & 3 & 1 \\ -2 & 1 & -2 \\ x & 1 & 0 \end{vmatrix}$$

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## #14 Theta Ciphering MA® National Convention 2016

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